

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■■■

ID: 91e7ea5e

3.1

$h(x) = 2(x - 4)^2 - 32$

The quadratic function h is defined as shown. In the xy -plane, the graph of $y = h(x)$ intersects the x -axis at the points $(0,0)$ and $(t,0)$, where t is a constant. What is the value of t ?

- A. 1
- B. 2
- C. 4
- ~~D. 8~~

Desmos → (0, 0), (8, 0)
(0, 0)

Question ID a9084ca4

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: a9084ca4

3.2

$$f(x) = 9,000(0.66)^x$$

The given function f models the number of advertisements a company sent to its clients each year, where x represents the number of years since **1997**, and $0 \leq x \leq 5$. If $y = f(x)$ is graphed in the xy -plane, which of the following is the best interpretation of the y -intercept of the graph in this context?

- A. ~~The minimum~~ estimated number of advertisements the company sent to its clients during the **5** years was **1,708**.
- B. ~~The minimum~~ estimated number of advertisements the company sent to its clients during the **5** years was **9,000**.
- C. The estimated number of advertisements the company sent to its clients in **1997** was ~~**1,708**~~.
- ~~D.~~ The estimated number of advertisements the company sent to its clients in **1997** was **9,000**.

Question ID b8f13a3a

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: b8f13a3a

3.3

Function f is defined by $f(x) = -a^x + b$, where a and b are constants. In the xy -plane, the graph of $y = f(x) - 12$ has a y -intercept at $(0, -\frac{75}{7})$. The product of a and b is $\frac{320}{7}$. What is the value of a ?

$$-\frac{75}{7} = -a^0 + b - 12$$

$$-\frac{75}{7} = -1 + b - 12 \quad \text{ระวังเครื่องหมาย}$$

$$b = \frac{16}{7}$$

$$ab = \frac{320}{7}$$

$$\frac{16}{7}a = \frac{320}{7}$$

$$a = 20 //$$

Question ID 7902bed0

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 7902bed0

$(1.8, 51.84), (3.6, 0)$

3.4

A machine launches a softball from ground level. The softball reaches a maximum height of 51.84 meters above the ground at 1.8 seconds and hits the ground at 3.6 seconds. Which equation represents the height above ground h , in meters, of the softball t seconds after it is launched?

A. $h = -t^2 + 3.6$

B. $h = -t^2 + 51.84$

C. $h = -16(t + 51.84)^2 - 3.6$

~~D. $h = -16(t - 1.8)^2 + 51.84$~~

Desmos

Question ID 4a0d0399

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 4a0d0399

3.5

The function f is defined by $f(x) = a^x + b$, where a and b are constants. In the xy -plane, the graph of $y = f(x)$ has an x -intercept at $(2, 0)$ and a y -intercept at $(0, -323)$. What is the value of b ?

$$\begin{aligned} 0 &= a^2 + b & \textcircled{1} \\ -323 &= \underbrace{a^0}_1 + b & \textcircled{2} \end{aligned}$$

$$\textcircled{2} \rightarrow b = -324 //$$

Question ID 9654add7

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 9654add7

3.6

$$f(x) = -500x^2 + 25,000x$$

The revenue $f(x)$, in dollars, that a company receives from sales of a product is given by the function f above, where x is the unit price, in dollars, of the product. The graph of $y = f(x)$ in the xy -plane intersects the x -axis at 0 and a . What does a represent?

- A. The revenue, in dollars, when the unit price of the product is \$0 ~~✗~~
- B. The unit price, in dollars, of the product that will result in maximum revenue ~~✗~~
- ~~✗~~ C. The unit price, in dollars, of the product that will result in a revenue of \$0
- D. The maximum revenue, in dollars, that the company can make ~~✗~~

Question ID 263f9937

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 263f9937

3.7

Growth of a Culture of Bacteria

Day	Number of bacteria per milliliter at end of day
1	2.5×10^5
2	5.0×10^5
3	1.0×10^6

A culture of bacteria is growing at an exponential rate, as shown in the table above. At this rate, on which day would the number of bacteria per milliliter reach 5.12×10^8 ?

- A. Day 5
- B. Day 9
- C. Day 11
- ~~D. Day 12~~

$$y = (2.5 \times 10^5) (2^{x-1})$$

$$5.12 \times 10^8 = 2.5 \times 10^5 \times 2^{x-1}$$

$$2.048 \times 10^3 = 2^{x-1}$$

$$x = 12 //$$

Question ID 18e35375

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 18e35375

3.8

$$f(x) = (x - 14)(x + 19)$$

The function f is defined by the given equation. For what value of x does $f(x)$ reach its minimum?

A. -266

B. -19

C. $-\frac{33}{2}$

~~D. $-\frac{5}{2}$~~

Desmos → $(-2.5, -272.25)$
//

Question ID 9afe2370

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 9afe2370

3.9

The population P of a certain city y years after the last census is modeled by the equation below, where r is a constant and P_0 is the population when $y = 0$.

$$P = P_0(1 + r)^y$$

If during this time the population of the city decreases by a fixed percent each year, which of the following must be true?

- A. $r < -1$ → P จะติดลบ จำนวนคนติดลบไม่ได้
- ~~B. $-1 < r < 0$~~
- C. $0 < r < 1$ ✗
- D. $r > 1$ ✗

Question ID 0121a235

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 0121a235

3.10

x	p(x)
-2	5
-1	0
0	-3
1	-1
2	0

ขาก

→ X intercept

→ Y intercept

→ X intercept

The table above gives selected values of a polynomial function p . Based on the values in the table, which of the following must be a factor of p ?

- A. ~~$(x-3)$~~
- B. ~~$(x+3)$~~
- C. ~~$(x-1)(x-2)$~~
- D. ~~$(x+1)(x-2)$~~

$$x = -1, 2 \rightarrow p = 0$$

แน่นอนว่าต้อง p ต้องมี $(x+1)(x-2)$
เป็น factor

$$p = (\text{factor})(\text{ก้อนอื่นๆ})$$

$$= (x+1)(x-2)(\text{ก้อนอื่นๆ})$$

$$x = -1 \rightarrow 0 = (-1+1)(-1-2)(\text{ก้อนอื่นๆ})$$

$$x = 2 \rightarrow 0 = (2+1)(2-2)(\text{ก้อนอื่นๆ})$$

Question ID 70753f99

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 70753f99

3.11

The function f is defined by $f(x) = (x+3)(x+1)$. The graph of f in the xy -plane is a parabola. Which of the following intervals contains the x -coordinate of the vertex of the graph of f ?

A. $-4 < x < -3$

~~B. $-3 < x < -1$~~

C. $1 < x < 3$

D. $3 < x < 4$

Desmos $\rightarrow (-2, -1)$
//

Question ID 58dcc59f

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 58dcc59f

3.12

A landscaper is designing a rectangular garden. The length of the garden is to be 5 feet longer than the width. If the area of the garden will be 104 square feet, what will be the length, in feet, of the garden?

$$L = W + 5$$

$$W(W + 5) = 104$$

$$W = 8, -\cancel{13}$$

$$W + 5 = \cancel{13}, -\cancel{8}$$

//

Question ID 84dd43f8

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 84dd43f8

3.13

For the function f , $f(0) = 86$, and for each increase in x by 1, the value of $f(x)$ decreases by 80%. What is the value of $f(2)$?

$$f(1) = 86(0.2) = 17.2$$

$$f(2) = 17.2(0.2) = 3.44 //$$

$$f(x) = 86(0.2)^x$$

$$f(2) = 86(0.2)^2$$

$$= 3.44 //$$

Question ID 59d1f4b5

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 59d1f4b5

3.14

$$M = 1,800(1.02)^t$$

The equation above models the number of members, M , of a gym t years after the gym opens. Of the following, which equation models the number of members of the gym q quarter years after the gym opens?

~~A. $M = 1,800(1.02)^{\frac{q}{4}}$~~

B. $M = 1,800(1.02)^{4q}$

C. $M = 1,800(1.005)^{4q}$

D. $M = 1,800(1.082)^q$

$$t = 1 \rightarrow q = 4$$

ทั้ง 2 สมการต้องเท่ากัน

หรือ $\frac{t}{1} \left(\frac{y}{y} \right) = \frac{t}{1 \times 4} \left(\frac{y}{y} \right)$

Question ID 01668cd6

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 01668cd6

3.15

The functions f and g are defined by the given equations, where $x \geq 0$. Which of the following equations displays, as a constant or coefficient, the maximum value of the function it defines, where $x \geq 0$?

I. $f(x) = 33(0.4)^{x+3}$

II. $g(x) = \underline{33(0.16)}(0.4)^{x-2}$
5.28

A. I only

~~B. II only~~

C. I and II

D. Neither I nor II

ใน II Max ต้องเป็นเฉพาะ $33/5.28/0.16$
 ? ยกกำลังใน Desmos ให้ได้วงเล็บ
 สหเจเฉพาะ Max Y ในช่วง $x \geq 0$
 Desmos $\rightarrow$ I. $Y_{\text{Max}} = 2.112$
 II. $Y_{\text{Max}} = \underline{33}$

Question ID 635f54ee

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■■■

ID: 635f54ee

3.16

หน้าอยู่ Topic 4

The surface area of a cube is $6\left(\frac{a}{4}\right)^2$, where a is a positive constant. Which of the following gives the perimeter of one face of the cube?

- A. $\frac{a}{4}$
- ~~B. a~~
- C. $4a$
- D. $6a$

cube มี 6 หน้า

1 หน้า มี พื้นที่ $\left(\frac{a}{4}\right)^2$

แต่จะแทนยาว = $\sqrt{\left(\frac{a}{4}\right)^2}$, ~~$-\sqrt{\left(\frac{a}{4}\right)^2}$~~

= $\frac{a}{4}$

ความยาวรอบรูป = $\left(\frac{a}{4}\right)4 = a //$

Question ID de39858a

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: de39858a

3.17

The function h is defined by $h(x) = a^x + b$, where a and b are positive constants. The graph of $y = h(x)$ in the xy -plane passes through the points $(0, 10)$ and $(-2, \frac{325}{36})$. What is the value of ab ?

- A. $\frac{1}{4}$
- B. $\frac{1}{2}$
- ~~C. 54~~
- D. 60

$$10 = a^0 + b$$

$$10 = 1 + b$$

$$b = 9$$

$$\frac{325}{36} = a^{-2} + 9$$

$$\frac{1}{36} = \frac{1}{a^2}$$

$$a = 6, \text{ } \cancel{-6}$$

$$ab = 6(9) \\ = 54 //$$

Question ID 1178f2df

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 1178f2df

3.18

x	y
21	-8
23	8
25	-8

Desmos สร้างสมการ

$$y = -4x^2 + 184x - 2108$$

The table shows three values of x and their corresponding values of y , where $y = f(x) + 4$ and f is a quadratic function. What is the y -coordinate of the y -intercept of the graph of $y = f(x)$ in the xy -plane?

Y-intercept of $y = -2,108$
 $-4 \rightarrow f(x) = -2,112$
 เพื่อให้เหลือแค่ $f(x)$

Question ID 84e8cc72

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 84e8cc72

Desmos กราฟสมการไม่ได้เพราะมีแค่ 2 จุด

A quadratic function models the height, in feet, of an object above the ground in terms of the time, in seconds, after the object is launched off an elevated surface. The model indicates the object has an initial height of 10 feet above the ground and reaches its maximum height of 1,034 feet above the ground 8 seconds after being launched. Based on the model, what is the height, in feet, of the object above the ground 10 seconds after being launched?

A. 234

B. 778

~~C. 970~~

D. 1,014

$$y = ax^2 + bx + \underline{10}$$

$$\frac{-b}{2a} = 8 \rightarrow b = \underline{-16a}$$

$$1,034 = 64a + 8b + 10$$

$$1,034 = 64a + 8(-16a) + 10$$

$$1,034 = -64a + 10$$

$$a = -16 \rightarrow b = -16a = -16(-16) = 256$$

$$y = -16x^2 + 256x + 10$$

$$y = -16(10)^2 + 256(10) + 10$$

$$= 970 //$$

Question ID 4b642eef

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 4b642eef

3.20

The total distance d , in meters, traveled by an object moving in a straight line can be modeled by a quadratic function that is defined in terms of t , where t is the time in seconds. At a time of 10.0 seconds, the total distance traveled by the object is 50.0 meters, and at a time of 20.0 seconds, the total distance traveled by the object is 200.0 meters. If the object was at a distance of 0 meters when $t = 0$, then what is the total distance traveled, in meters, by the object after 30.0 seconds?

Handwritten notes and arrows:

- $(10, 50)$ with an arrow pointing to "total distance traveled by the object is 50.0 meters"
- $(20, 200)$ with an arrow pointing to "total distance traveled by the object is 200.0 meters"
- $(0, 0)$ with an arrow pointing to "distance of 0 meters when $t = 0$ "

Desmos → สร้างสมการ
มี 3 จุด

$$y = 0.5x^2$$

$$y = 0.5(30)^2$$

$$= 450 //$$

Question ID 9f2ecade

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 9f2ecade

3.21

$$h(x) = x^3 + ax^2 + bx + c$$

The function h is defined above, where a , b , and c are integer constants. If the zeros of the function are -5 , 6 , and 7 , what is the value of c ?

↖ x-intercept

$$y = (x + 5)(x - 6)(x - 7)$$

$$c = 5(-6)(-7)$$

$$= 210$$

//

Question ID 6f5540a5

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 6f5540a5

3.22

Kao measured the temperature of a cup of hot chocolate placed in a room with a constant temperature of 70 degrees Fahrenheit ($^{\circ}\text{F}$). The temperature of the hot chocolate was 185°F at 6:00 p.m. when it started cooling. The temperature of the hot chocolate was 156°F at 6:05 p.m. and 135°F at 6:10 p.m. The hot chocolate's temperature continued to decrease. Of the following functions, which best models the temperature $T(m)$, in degrees Fahrenheit, of Kao's hot chocolate m minutes after it started cooling?

A. $T(m) = 185(1.25)^m$

B. $T(m) = 185(0.85)^m$

C. $T(m) = (185 - 70)(0.75)^{\frac{m}{5}}$

~~D. $T(m) = 70 + 115(0.75)^{\frac{m}{5}}$~~

แทนค่า $(0, 185)$ //
 $(5, 156)$
 $(10, 135)$

Question ID b73ee6cf

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: b73ee6cf

3.23

The population of a town is currently 50,000, and the population is estimated to increase each year by 3% from the previous year. Which of the following equations can be used to estimate the number of years, t , it will take for the population of the town to reach 60,000 ?

A. $50,000 = 60,000(0.93)^t$

B. $50,000 = 60,000(3)^t$

C. $60,000 = 50,000(0.93)^t$

~~D. $60,000 = 50,000(1.03)^t$~~

Question ID 7eed640d

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 7eed640d

3.24

$$h(x) = -16x^2 + 100x + 10$$

The quadratic function above models the height above the ground h , in feet, of a projectile x seconds after it had been launched vertically. If $y = h(x)$ is graphed in the xy -plane, which of the following represents the real-life meaning of the positive x -intercept of the graph?

- A. The initial height of the projectile y-intercept
- B. The maximum height of the projectile ✗
- C. The time at which the projectile reaches its maximum height ✗
- ✗ D. The time at which the projectile hits the ground x-intercept

Question ID 43926bd9

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 43926bd9

3.25

x	$f(x)$
1	a
2	a^5
3	a^9

For the exponential function f , the table above shows several values of x and their corresponding values of $f(x)$, where a is a constant greater than 1. If k is a constant and $f(k) = a^{29}$, what is the value of k ?

lnn $a = \underline{2}, 3, \dots$

Desmos $\rightarrow y = 0.125 \times 16^x$

lnn $a = 2$

$2^{29} = 0.125 (16)^k$

$k = 8 //$

Question ID a7711fe8

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: a7711fe8

3.26

What is the minimum value of the function f defined by $f(x) = (x-2)^2 - 4$?

~~A. -4~~

B. -2

C. 2

D. 4

Desmos $\rightarrow$ (2, -4)
//

Question ID 1a722d7d

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 1a722d7d

3.27

Let the function p be defined as $p(x) = \frac{(x-c)^2 + 160}{2c}$, where c is a constant. If $p(c) = 10$, what is the value of $p(12)$?

- A. 10.00
- B. 10.25
- C. 10.75
- ☒ D. 11.00

$$10 = \frac{0^2 + 160}{2c}$$

$$c = 8$$

$$p(x) = \frac{(x-8)^2 + 160}{16}$$

$$p(12) = 11 //$$

Question ID 70fb357b

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: 70fb357b

3.28

$y = 576^{(2x+2)}$

The graph of the given equation in the xy-plane has a y-intercept of (r, s) . Which of the following equivalent equations displays the value of s as a constant, a coefficient, or the base?

~~A. $y = 331,776^{x+1}$~~

B. ~~$y = 2^{4x+4}$~~

C. $y = \frac{1}{24}(13,824)(576)^{2x}$

D. ~~$y = \frac{1}{576} 576^{(2x+3)}$~~

$S = 0$

แทน $x = 0$

X เพราะไม่ใช่สมการเดียวกัน
กับสมการต้นแบบ

$(\infty, 0)$

$y = 331,776$

$y = 331,776$

$y = 576$

$y = 331,776$

Question ID 1073d70c

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 1073d70c

3.29

At the time that an article was first featured on the home page of a news website, there were 40 comments on the article. An exponential model estimates that at the end of each hour after the article was first featured on the home page, the number of comments on the article had increased by 190% of the number of comments on the article at the end of the previous hour. Which of the following equations best represents this model, where C is the estimated number of comments on the article t hours after the article was first featured on the home page and $t \leq 4$?

- A. $C = 40^{(1.19)^t}$
- B. $C = 40^{(1.9)^t}$
- C. $C = 40^{(19)^t}$
- ☒ D. $C = 40^{(2.9)^t}$

Question ID 7a6d06bf

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 7a6d06bf

၁၇၀၅၂ Topic 4

3.30

A rectangle has an area of **155** square inches. The length of the rectangle is **4** inches less than **7** times the width of the rectangle. What is the width of the rectangle, in inches?

$155 = LW$

$L = 7W - 4$

Desmos $\rightarrow (W, L)$

$\rightarrow (\underset{//}{5}, 31), (\underset{\times}{-4.42857}, \underset{\times}{-35})$

Question ID 270cf326

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 270cf326

3.31

Which of the following functions has(have) a minimum value at -3 ?

$f(x) = -6(3)^x - 3$
I.

$g(x) = -3(6)^x$
II.

- A. I only
- B. II only
- C. I and II
- ~~D. Neither I nor II~~

Desmos $\rightarrow$ I. $y_{\text{MIN}} = -\infty$
II. $y_{\text{MIN}} = -\infty$

Question ID ce508fb0

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	■ ■ ■

ID: ce508fb0

3.32

The functions f and g are defined by the given equations. $f(x) = 3 + | - 2x - x^2 |$ $g(w) = | \frac{-w}{w-1} | - w + 5$
If $f(-4) = c$, where c is a constant, what is the value of $g(c)$?

$$\begin{aligned} f(-4) &= 3 + | - 2(-4) - (-4)^2 | \\ &= 3 + | - 8 | \\ &= 11 \\ g(11) &= \left| \frac{-11}{11-1} \right| - 11 + 5 \\ &= | -1.1 | - 11 + 5 \\ &= -4.9 \end{aligned}$$

Question ID 2992ac30

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Advanced Math	Nonlinear functions	

ID: 2992ac30

3.33

$P(t) = 260(1.04)^{(\frac{t}{4})}$

The function P models the population, in thousands, of a certain city t years after 2003. According to the model, the population is predicted to increase by 4% every n months. What is the value of n ?

- ~~A. 8~~
- B. 12
- C. 18
- D. 72

$$260(1.04)^{\frac{t}{\frac{4}{6} \times 12}} = 260(1.04)^{\frac{t}{n}}$$
$$\frac{t}{8} = \frac{t}{n}$$
$$n = 8 //$$